

An Autonomous Proximity Navigation Testbed for Nanosatellites

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ABSTRACT

The goal of this work is to develop techniques and tools to enhance small-spacecraft in-orbit autonomy. The focus is on developing perception and control algorithms to enable autonomous proximity operations, and performing preliminary validation in a laboratory air-bearing testbed. To achieve this, we have developed cubesat engineering models equipped with a simple cold-gas propulsion system, on-board vision-based sensing and embedded computer for perception and control algorithms, and integrated them in the air-bearing testbed. Basic point-to-point autonomous navigation and obstacle avoidance tasks in such a planar environment have been successfully demonstrated.

INTRODUCTION

Recent developments in the area of small satellites [1], [2], [3] have resulted in new classes of *pico-satellites* and *nano-satellites*, weighing less than 1 kg and 10 kg, respectively, that enable low-cost missions due to reduced size and weight requirements, unified standard resulting in collaborative world-wide (partially open-source) effort [4], [5], and increase in launch opportunities. Currently, there is active research in improving basic functionalities such as attitude control [6], as well as developing more advanced capabilities including formation flying [7] and proximity operations [8], [9].

This work is concerned with autonomous navigation in a close proximity (e.g. 10 meters) of a target object. Such navigation requires the ability of the spacecraft to construct a spatial representation of its surrounding and to generate obstacle-free trajectories to a desired state while optimizing a given performance metric such as fuel expended or time taken. Autonomous navigation thus inherently relies on real-time perception, spatial mapping, path planning, and trajectory control with real-time feedback from on-board sensing. In addition, hardware limitations such as control input bounds, mass and power budget further complicate the problem.

Our main focus is on the development of control algorithms for trajectory generation and obstacle avoidance, and the integration of these algorithms with perception algorithms for a complete navigation system. To validate such complex technology it is necessary to perform extensive laboratory testing of both the hardware components and software algorithms. Motivated by this need, we have also designed and built an air-bearing test-bed together with a Cubesat engineering model for partial validation of these algorithms.

Employing frictionless air-bearing testbeds is a standard

approach [10], [11], [12], [13] for system validation, typically allowing three (translation in the plane and rotation around the vertical axis) or five (translations in the plane and any rotation within a given range) degrees of freedom. While very common for larger spacecraft, few such testbeds exist specifically for cubesat or smaller form-factor spacecraft. One reason has been the unavailability of inexpensive and easy-to-use propulsion system that is safe to use in a laboratory environment. We have, therefore, designed a simplified cold gas propulsion system suitable for safe testing in a laboratory environment without the need for special protective equipment. The approach is based on rapid-prototyping inspired by recent 3D-printed integrated propulsion systems [14], [15].

An overview of the testbed is given next, followed by a description of the hardware and software components, with particular focus on the perception algorithms, and the novel control and obstacle avoidance methods. Finally, we present experimental results of autonomous navigation through a mock-up air-table environment with obstacles.

TESTBED OVERVIEW

The testbed consists of three main components: a cubesat engineering model placed on an air-bearing base, a flat granite table, and a motion capture system for providing ground truth data. The setup permits three degree-of-freedom motions, two translational on the table and one rotational around the vertical axis. Mock-up obstacles representing other spacecraft or debris are positioned on the table. The testbed is enclosed in a housing assembled using aluminum framing and acrylic to create a clean environment with minimum external disturbances. Additional cameras are also employed to record experiments.



Fig. 1. The JHU Cubesat proximity navigation testbed.

HARDWARE DESIGN

The cubesat engineering model hardware consists of a propulsion subsystem, power subsystem, sensing and computing components. The details of each subsystem are presented in the subsections below. The model was designed from ground up with the dimensions of 3U cubesat in mind. We chose not to use any commercially available housing because it would need to be extensively modified to allow for assembly of non standard component.

We have followed a modular design that facilitates frequent assembly and disassembly, and allows introduction of modification with ease. The Cubesat engineering model also houses a CO₂ canister(68 g and an adjustable regulator on-board. A cylindrical hole in the center on the manifold allows a compact assembly in the frame. A switchable 2-way valve is integrated to be choose the CO₂ supply between the onboard CO₂ canister and an external compressed air source. The external compressed air is provided through a flexible pipe which connect to a quick disconnect coupling at the top of the model. The external compressed air source is meant to



Fig. 2. The Cubesat engineering model with components related to autonomous proximity navigation.

be used during testing phase as it adds significant external forces to the model. The onboard CO₂ supply lasts for about 7 minutes of continuous use. The model is powered by a 7.4 V 4 Ah battery which powers it for about 30 minutes.

The detail list of the hardware components are presented in the table:I. The further details of the hardware design are as follows:

Propulsion Subsystem

The propulsion sub system consists of a 3D printed manifold, pneumatic solenoid valves and an one way valve. Although the design is based on other 3D printed propulsion system that can store and utilize liquid compressed gas, this design takes in CO₂ at 60 PSI from a canister on-board which is same one used by the air-bearing components. We decided to use CO₂ to facilitate prolonged laboratory testing and ensure safety of people involved. Experiments conducted have shown. Although the thrust varies from one thruster to another, experiments conducted put the the average maximum thrust at around 0.1N. The nozzles and the propellant

TABLE I
LIST OF KEY AUTONOMY HARDWARE COMPONENTS.

Name	Description	Specification
Advantech MIO-2262	High-level computer	CPU: Atom N2800
ATmega 2560	Low-level controller	CPU: 8-bit AVR
		Architecture:RISC Freq: 16 MHz SRAM: 256 Kbytes
Hokuyo URG-04LX	Lidar	Max range: 1000 mm Min range: 20 mm Resolution: 2 mm
ASUS Xtion Pro	Depth sensor	Max range: 4.5 m
Minoru camera	Stereo camera	Baseline: 10 mm FOV:72°
MPU 6000	IMU unit	Interface: SPI Accl range: $\pm 4g$ Accl res: 16 bit Gyro Range: $\pm 500^\circ$ Gyro res: 16 bit
Parker X-Valve	Solenoid Valves	Max pressure: 100 psi
Li-ion battery	Onboard Power	Cells: 2 Capacity: 4000mAh
Newway S102501	Air bearing	Flatness: 0.0005 mm Size: 25 mm dia

manifold is designed and manufactured using a type of rapid prototyping technique call Polyjet Printing. The advantage of polyjet printing is that the parts can be printed in very high resolution and that they are non-porous. The cost of printing is significantly lower than other rapid prototyping techniques.

Figure ?? shows the propulsion system assembly. A cutaway portion reveals the nozzle design.

Sensing and Computing Components

The sensing and computing components includes several sensors, a low-level controller and a high level computer. The information flow is described in Figure 5

The processing for autonomy algorithm takes place on the The motion of the cubesat model is captured externally using a commercial motion capture system and is used as ground-truth for comparison

1) *Sensors*: The engineering model is instrumented with several sensors for collecting the inertial measurement data, monitoring parameters like the pressure, temperature of CO₂, total current consumption and battery voltage. In addition, there are sensors like laser scanner,

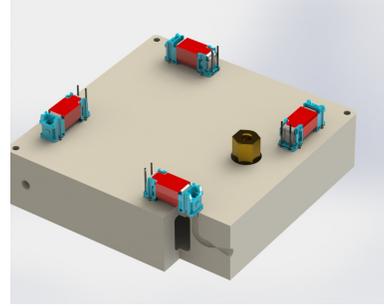


Fig. 3. 3D printed propulsion manifold assembled with low-cost solenoid pneumatic valves.

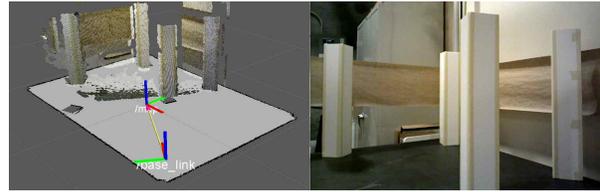


Fig. 4. Left: Point cloud from Depth sensor Right: Camera view.

depth cameras and stereo cameras which communicate with the high-level computer. Depth cameras provide depth information aligned with every pixel, in addition to the color information of an image pixel, that is robust to lighting condition and textures of objects in view.

2) *Low-level Controllers*: The low-level controller is an AVR microcontroller based board which controls the solenoid valves, communicates with sensors and high-level computer, and runs low level estimation and control algorithms.

3) *High-Level Computer*: MIO-2262, an Intel Atom N2800 based SBC, is used as the high-level computer. It interfaces to a pair of stereo vision cameras, PrimeSense depth camera and a low level controller board. The low-level controller is an AVR microcontroller based board which controls the solenoid valves, communicates with sensors and high-level computer, and runs low level estimation and control algorithms.

ROBOT OPERATING SYSTEM(ROS) BASED SOFTWARE ARCHITECTURE

Our approach is to build upon and extend existing robotic algorithms, specifically related to robot perception, trajectory planning and control. The Robot Operating System (ROS) is a set of open-source robotic software libraries and tools which provide a subset of these required capabilities. We utilized the existing perception algorithms for mapping and localization in ROS and developed novel control and obstacle avoidance methods specifically for nanosatellites. These new al-

gorithms are also integrated within the ROS framework which is also used for visualization and user interface. The details of the algorithms are discussed next.

PERCEPTION ALGORITHM

The spacecraft sensor data is processed using perception algorithms that generate a map of the environment and localize the spacecraft with respect to this map. Data from the Inertial Measurement Unit (IMU), camera images and laser scans of satellite's surrounding, as well the thruster commands serve as inputs to the algorithm. We assume that the shape of obstacles is known, so that they can be easily identified in the constructed map. The pose of the physical obstacles is then employed by the control algorithm to navigate to the goal while avoiding collisions.

Different algorithms are employed based on the sensor type, i.e. whether a 3-D depth camera or a 2-D Lidar is used. For depth-cameras we use an open-source algorithm, RGBD-SLAM [16], based on 3-d feature matching and relative pose estimation. Local maps and their relative transformations are combined as a graph which is further optimized to produce a consistent global 3D map. For laser scanners we employ a traditional occupancy-grid based simultaneous localization and mapping (SLAM) and particle filter (PF) localization. The map in the SLAM algorithm is a grid where the value of each cell is related to the probability of the grid being occupied. Multiple possible maps are maintained as particles in a probabilistic representation accounting for uncertainty. Our implementation is based on the open-source Gmapping [17] for mapping and AMCL [18] for localization.

CONTROL ALGORITHM

We employ gyroscopic obstacle avoidance algorithm combined with standard stabilization control laws to handle unexpected obstacles during trajectory execution. Our approach is motivated by the fact that gyroscopic forcing has desirable convergence properties under certain conditions. In particular, the system is guaranteed to avoid collisions and reach the goal as long as the obstacle is convex and the required controls do not saturate.

Avoiding collisions is a key requirement for autonomous proximity operations. The subject has a long history in robotics (see [19] and [20] for an overview). Standard methodologies include potential fields [21], artificial navigation functions [22], or dynamic window avoidance [23]. Gyroscopic avoidance [24], employed in this work, is another strategy based on steering away from obstacles without injecting additional energy (e.g. from repulsive potential forces) into the system. By designing the system to have minimum energy at a given

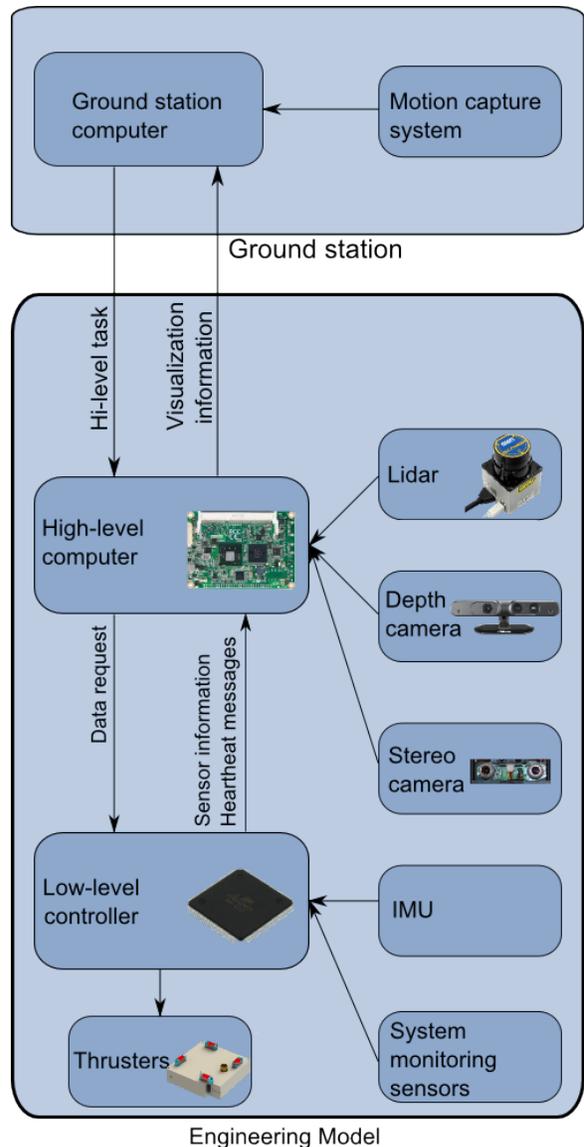


Fig. 5. Sensor, actuator, and computing components.

goal state, the system is guaranteed to reach that state even in presence of obstacles.

System Model

The robot is modeled as a single rigid body with position $\mathbf{x} = (x, y, z) \in \mathbb{R}^3$ and orientation matrix $R \in SO(3)$ defined with respect to a moving frame attached to a nearby moving reference (e.g. a target), such as an RSW frame [25], [26]. The *body-fixed* angular velocity is denoted by $\boldsymbol{\omega} \in \mathbb{R}^3$. The vehicle has mass m and principal moments of rotational inertia J_x, J_y, J_z forming the inertia tensor $\mathbb{J} = \text{diag}(J_x, J_y, J_z)$.

The spacecraft is actuated with c thrusters producing forces denoted by $\mathbf{u} \in U$ where $U \subset \mathbb{R}^c$ is a bounded

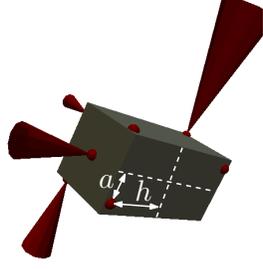


Fig. 6. The ten-thruster configuration for full 6-dof control.

set. The equations of motion are

$$\dot{R} = R\hat{\omega}, \quad (1)$$

$$\begin{pmatrix} \mathbb{J}\dot{\omega} \\ m\ddot{\mathbf{x}} \end{pmatrix} = \begin{pmatrix} \mathbb{J}\omega \times \omega + \tau_{\text{ext}} \\ \mathbf{f}_{\text{ext}} \end{pmatrix} + \begin{bmatrix} \mathbf{1} & \mathbf{0} \\ \mathbf{0} & R \end{bmatrix} B\mathbf{u}, \quad (2)$$

where the map $\hat{\cdot}: \mathbb{R}^3 \rightarrow \mathfrak{so}(3)$ is defined by

$$\hat{\omega} = \begin{bmatrix} 0 & -\omega_z & \omega_y \\ \omega_z & 0 & -\omega_x \\ -\omega_y & \omega_x & 0 \end{bmatrix}, \quad (3)$$

and B is a constant thruster allocation matrix such that $\text{rank}(B) = 6$ and $\{B\mathbf{u} \mid \mathbf{u} \in U\} \subset \mathbb{R}^6$ is an open set containing the origin.

For our satellite equipped with ten thrusters illustrated in Figure 6 the thruster allocation matrix is defined by

$$B = \begin{bmatrix} 0 & -h & 0 & h & h & 0 & -h & 0 & 0 & 0 \\ h & 0 & -h & 0 & 0 & h & 0 & -h & 0 & 0 \\ a & a & a & a & -a & -a & -a & -a & 0 & 0 \\ -1 & 0 & 1 & 0 & 0 & 1 & 0 & -1 & 0 & 0 \\ 0 & -1 & 0 & 1 & -1 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & -1 \end{bmatrix},$$

where $a > 0$ and $h > 0$ are the lateral and vertical offsets of each of the side thrusters. A standard approximation of external forces is

$$\mathbf{f}_{\text{ext}} = m \begin{bmatrix} 2\omega_c \dot{z} \\ -\omega_c^2 y \\ -2\omega_c \dot{x} + 3\omega_c^2 z \end{bmatrix},$$

with constant $\omega_c > 0$ denoting the circular orbit angular rate. The dominating torques are due to gravity gradients defined by

$$\tau_{\text{ext}} = 3\omega_c^2 R\mathbf{e}_z \times \mathbb{J}R\mathbf{e}_z,$$

where $\mathbf{e}_z = (0, 0, 1)$. Given the time-scales considered in this work (e.g. maneuvers lasting on the order of a few minutes) the effect of such forces is negligible.

Obstacle constraints require that the spacecraft must not collide with obstacles denoted by $\mathcal{O}_1, \dots, \mathcal{O}_{n_o} \subset \mathbb{R}^3$. Assume that the vehicle is occupying a region $\mathcal{A}(R, \mathbf{x}) \subset \mathbb{R}^3$, and let $\mathbf{prox}(\mathcal{A}_1, \mathcal{A}_2)$ be the Euclidean

distance between two sets $\mathcal{A}_{1,2}$ that is negative in the case of intersection. Obstacle avoidance requires that

$$\min_i \mathbf{prox}(\mathcal{A}(R, \mathbf{x}), \mathcal{O}_i) > 0. \quad (4)$$

We use a standard collision checking algorithm implemented by Proximity Query Package (PQP) [27] to compute \mathbf{prox} .

Gyroscopic Obstacle Avoidance

The goal of gyroscopic steering is to modify the dynamical system so that obstacles are avoided without violating its stability properties. This is accomplished by adding a gyroscopic force term, i.e. that does not inject energy into the system. Our development in this context can be regarded as an extension of [24] to 3-D workspaces and to vehicles with more realistic dynamics.

Assume that while executing a reference trajectory $\mathbf{x}_r: [0, T] \rightarrow \mathbb{R}^3$ at time $t < T$ the vehicle encounters an unexpected obstacle blocking its path. Obstacle avoidance is performed by first assigning a new desired position state $(\mathbf{x}_d, \dot{\mathbf{x}}_d)$, for instance $\mathbf{x}_d = \mathbf{x}_r(t_g)$ for some $t < t_g \leq T$ and then steering away from the obstacle and towards \mathbf{x}_d . This is accomplished by defining the error term

$$\Delta \mathbf{x} = \mathbf{x} - \mathbf{x}_d$$

and the control law

$$\mathbf{f}_d = -k_x \Delta \mathbf{x} - k_v \Delta \dot{\mathbf{x}} - \mathbf{f}_{\text{ext}} + \Gamma \dot{\mathbf{x}}, \quad (5)$$

where $k_x, k_v > 0$ and $\Gamma \in \mathbb{R}^{3 \times 3}$ is a skew-symmetric matrix, i.e. such that $\Gamma = -\Gamma^T$.

Let $d(R, \mathbf{x}) > 0$ and $\mathbf{n}(R, \mathbf{x}) \in \mathbb{R}^3$ denote the distance and the unit vector to the detected obstacle, respectively, computed by the \mathbf{prox} function. We then set

$$\Gamma = \frac{k_g v_{\text{max}}}{d(R, \mathbf{x})} \hat{\mathbf{c}}, \quad (6)$$

for some fixed $k_g, v_{\text{max}} > 0$, and $\mathbf{c} \in \mathbb{R}^3$ is computed according to

$$\mathbf{c} = \begin{cases} 0 & \text{if } |\beta| \geq \pi/2, \\ \frac{\mathbf{c}'}{\|\mathbf{c}'\|} & \text{if } |\beta| < \pi/2, \end{cases} \quad (7)$$

$$\mathbf{c}' = \frac{\mathbf{n} \times \dot{\mathbf{x}}}{\|\dot{\mathbf{x}}\|},$$

$$\beta = \text{sgn}(\arcsin \|\mathbf{c}'\|) \arccos \frac{\mathbf{n}^T \dot{\mathbf{x}}}{\|\dot{\mathbf{x}}\|}.$$

Here $\beta \in [-\pi, \pi]$ is angle between direction of collision and direction of motion, and \mathbf{c} plays the role of an axis around which the velocity vector $\dot{\mathbf{x}}$ rotates to avoid the obstacle.

Control Law

We next design a controller to track desired position $\mathbf{x}_d(t)$ and attitude $R_d(t)$ during a time interval $[0, T]$, which must be chosen so that the required control inputs do not saturate. Asymptotic stability can be achieved by setting the controls to

$$\mathbf{u} = (B^T B)^{-1} B^T \begin{bmatrix} \boldsymbol{\tau}_d \\ R^T \mathbf{f}_d \end{bmatrix}, \quad (8)$$

where \mathbf{f}_d is defined in (5) and $\boldsymbol{\tau}_d$ is a standard attitude tracking control law. For instance, following [28] such a control law is obtained by

$$\begin{aligned} \boldsymbol{\tau}_d = & -\text{skew}(K_R \Delta R) \overset{\sim}{-} K_\omega (\boldsymbol{\omega} - \Delta R^T \boldsymbol{\omega}_d) \\ & + \boldsymbol{\omega} \times \mathbb{J}(\Delta R^T \boldsymbol{\omega}_d) + \mathbb{J}(\Delta R^T \dot{\boldsymbol{\omega}}_d), \end{aligned} \quad (9)$$

where $\Delta R := R_d^T R$, $\text{skew}(A) := (A - A^T)$, the operator $\overset{\sim}{-}$ is the inverse of $\hat{\cdot}$ defined in (3), and K_R, K_ω are positive definite matrices.

The complete algorithms is summarized below:

Algorithm 1: $\mathbf{u} = \text{Track}(\mathbf{x}(t), R(t), \mathbf{x}_d(t), R_d(t))$

parameters: gains $k_x, k_v, K_R, K_\omega, k_g$

- 1 $\mathbf{f}_d = -k_x \Delta \mathbf{x} + k_v \Delta \dot{\mathbf{x}} - \mathbf{f}_{\text{ext}}(\mathbf{s}) + \Gamma \dot{\mathbf{x}}$
 - 2 $\boldsymbol{\tau}_d = -\text{skew}(K_R \Delta R) \overset{\sim}{-} K_\omega (\boldsymbol{\omega} - \Delta R^T \boldsymbol{\omega}_d) + \boldsymbol{\omega} \times \mathbb{J}(\Delta R^T \boldsymbol{\omega}_d) + \mathbb{J}(\Delta R^T \dot{\boldsymbol{\omega}}_d)$,
 - 3 $\mathbf{u} = (B^T B)^{-1} B^T \begin{bmatrix} \boldsymbol{\tau}_d \\ R^T \mathbf{f}_d \end{bmatrix}$,
 - 4 **return** control inputs \mathbf{u}
-

Simulations in 3-D

Figure 7 shows an example scenario requiring the satellite to avoid a large obstacle to stabilize at the origin. The stabilization of a group of seven satellites performing a simulated segmented mirror assembly task is considered next. The goal is to reconfigure from a free-flying mode to a latched configuration without incurring any collisions. Figure (8) shows a few snapshots of the scenario. The algorithm exhibited good behavior and no collision happened before the final latching.

EXPERIMENTAL EVALUATION

The experiment was designed to simulate autonomous navigation of a single 3U CubeSat in the proximity of other mock-up spacecraft and objects treated as obstacles. The ground station, connected to the high-level onboard-computer, commands a desired goal position to the model which then autonomously navigates to the commanded position while avoiding the obstacles. We present, in Figure 9 and 10, the results as navigation and obstacle avoidance maneuvers for two goal position.

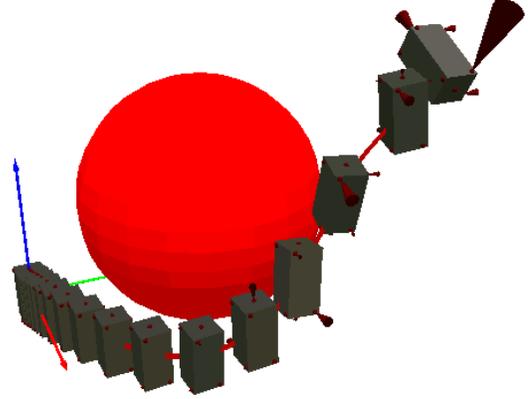


Fig. 7. A conceptual nanosatellite with ten thrusters avoiding a spherical obstacle and stabilizing at the origin.

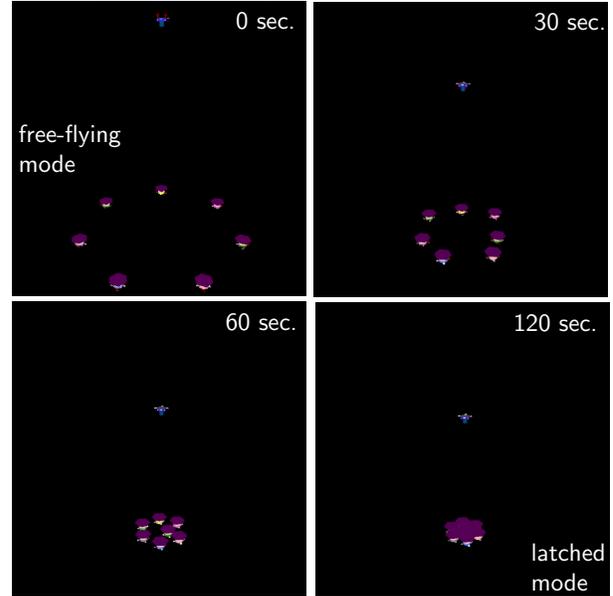


Fig. 8. Reconfiguration of a fleet of spacecraft forming a segmented mirror. Each vehicle employs gyroscopic obstacle avoidance to avoid collisions with other mock-up spacecraft and arriving stably at its latching configuration.

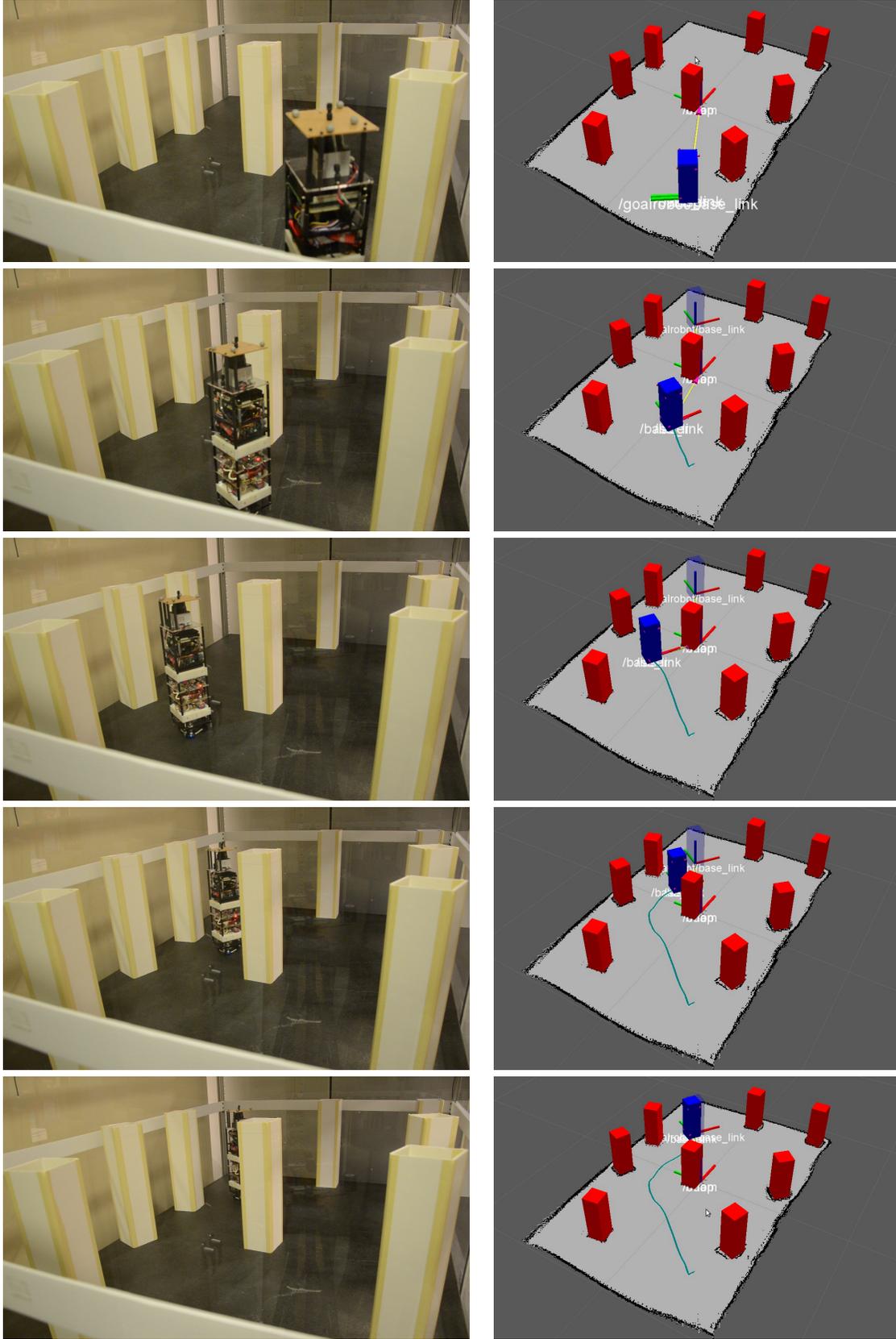


Fig. 9. Obstacle avoidance case 1

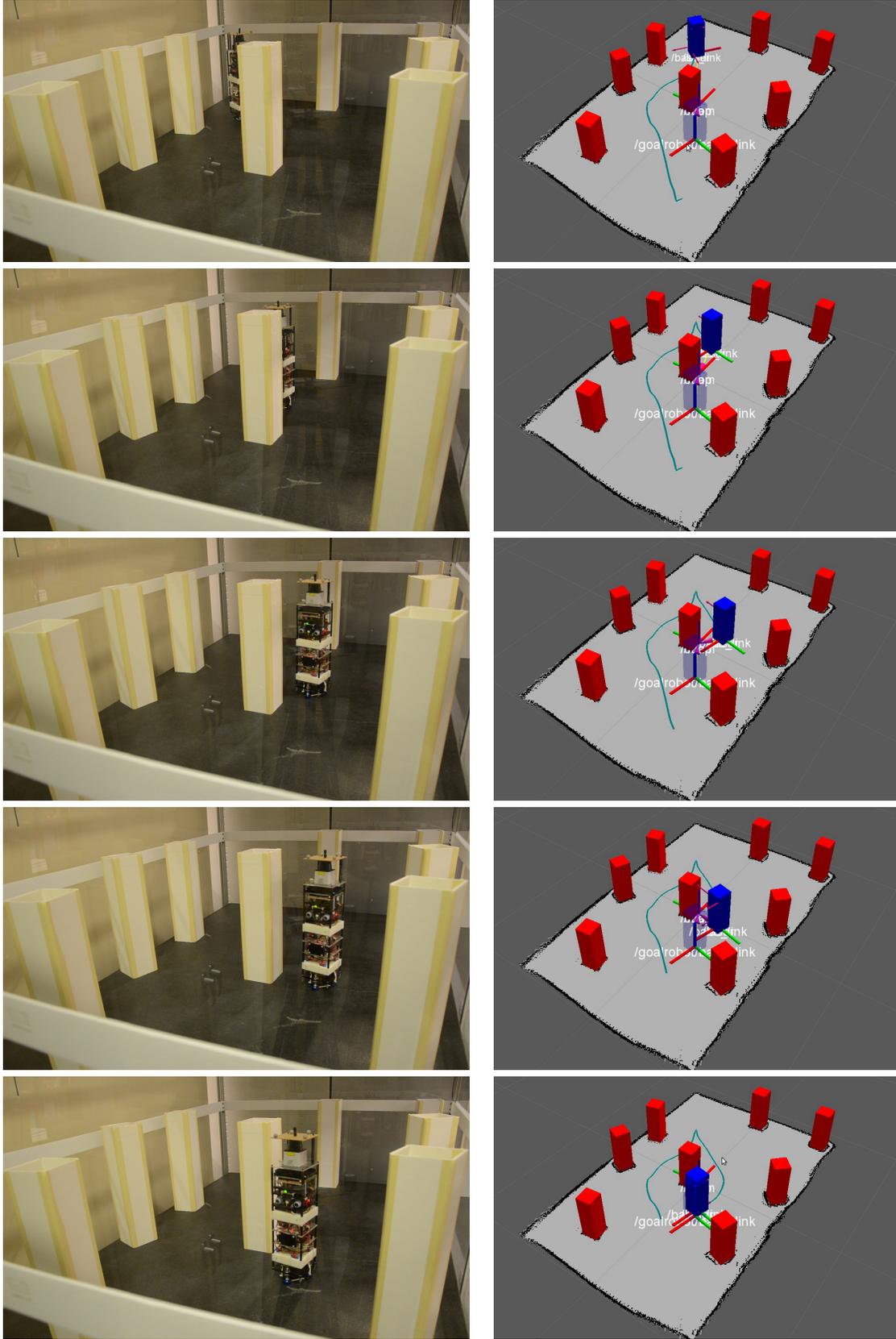


Fig. 10. Obstacle avoidance case 2

CONCLUSION AND FUTURE WORK

This work focused on the development and demonstration of autonomous proximity navigation capabilities for nano-satellites. The reported initial developments are based on a laboratory air-bearing testbed in which we were able to implement and test spacecraft perception, control, and obstacle avoidance algorithms. To achieve this we assumed a planar environment and employed a simplistic cold-gas propulsion system and embedded system components (which are yet to be validated in a space environment) with CPU computing power capable of executing current robotic perception and control algorithms. Future work will focus on employing 3-dof attitude control, a more realistic propulsion system, and performing integration with standard cubesat subsystems. Finally, our goal is to employ the developed algorithms to enable future applications across multiple spacecraft in mission-specific contexts such as satellite docking and servicing, debris removal, or small-body sampling.

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